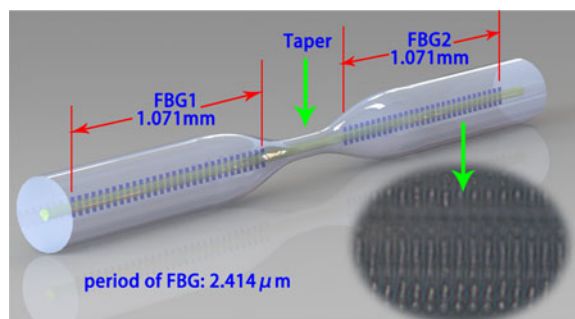


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Abstract: We demonstrate a phase-shifted fiber Bragg grating with a taper induced by femtosecond laser micromachining. In this configuration, a fiber taper fabricated by an arc discharge in a fiber splicer was sandwiched between two fiber Bragg grating sections, which were formed using femtosecond laser line-by-line inscription. The degree of phase shift produced by this device can be adjusted by introducing axial strain, with a sensitivity of 4.59 pm/ $\mu\epsilon$. A theoretical study was also conducted by modeling the taper under axial strain. The relative deviation between simulated and measured sensitivities is less than 10%.

Index Terms: Fiber Bragg gratings, fiber optics sensors, phase-shift.

1. Introduction

The first phase-shifted fiber Bragg grating (PS-FBG) was introduced in 1990 [1]. It has since been widely used in the fields of all-optical switching [2], wavelength demultiplexing [3], all-optical logic gating [4], optical temporal integration [5], and narrowband fiber filtering [6]. It has also been used to produce tunable wavelength devices [7] and fiber sensors for strain, liquid refractive index, acceleration, and temperature measurements [7]–[12].

Several techniques for fabricating PS-FBGs have been reported in the literature. One common approach employs a phase-shifted phase mask in single exposure [4], [13]–[16]. However, this technique has poor flexibility for changing the grating wavelength. PS-FBGs can be fabricated

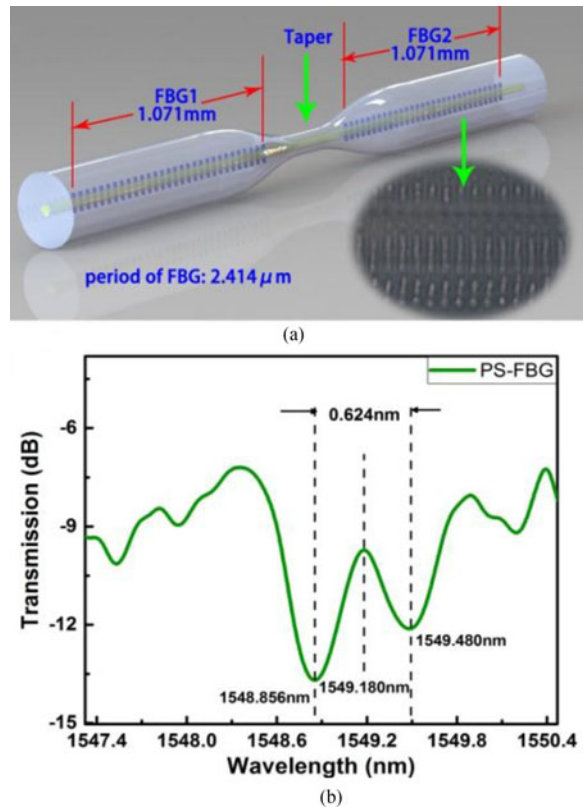


Fig. 1. (a) A schematic diagram of the proposed PS-FBG, with the taper sandwiched between two identical FBGs. (b) The transmission spectrum of one representative PS-FBG.

using the Moire method, a transverse holographic double-exposure technique [17]. The overlaid FBG method [18] is also effective but it requires complex equipment and an exact optical light path. Some authors have attempted to sandwich certain functional structures between two FBGs, i.e., an in-grating bubble [7] fabricated with femtosecond laser-assisted fusion splicing and a microchannel fabricated using either chemical [8] or plasma etching [19]. Although phase shift is tunable for these PS-FBG types, they degrade the integrality of the fiber, which introduces large insertion loss.

In this study, we propose and experimentally demonstrate a novel PS-FBG which includes a taper. Two identical FBGs are inscribed on each side of this taper. Two interesting phenomena have been observed during the axial strain applied to this PS-FBG. First, we found the degree of phase shift in the PS-FBG could be precisely adjusted by varying the axial strain. Secondly, we found the axial-strain sensitivity of the phase-shifted wavelength increased with decreasing taper diameter. A theoretical simulation was also conducted by modeling the taper under axial strain, the results of which were in good agreement with experiment.

2. Device Fabrication

Fig. 1(a) shows a schematic diagram for the proposed PS-FBG, including an inserted optical microscope image of the fabricated FBG. A single-mode fiber (SMF) was first tapered using an arc discharge in a fiber splicer. Two identical FBGs were then inscribed on each side of the taper using femtosecond laser line-by-line inscription. In this manner, the laser point was fixed and the fiber was first translated along the radial direction of the fiber with the intended velocity and distance. After inscription of the first grating pitch, the laser beam was blocked and the fiber was then moved to the starting point of the next grating pitch, after which the cycle was repeated.

TABLE 1
Samples Sizes

Sample Number	Taper Length (μm)	Minimum Fiber Core Diameter (μm)
1	0	9
2	300	4.6
3	480	2.2

Fig. 1(b) shows the transmission spectrum for one representative PS-FBG with a taper length of $\sim 300 \mu\text{m}$ and a minimum fiber core diameter of $\sim 4.6 \mu\text{m}$. During PS-FBG inscription, the pulse energy of the femtosecond laser was attenuated to $\sim 130 \text{ nJ}$ by rotating a half-wave plate followed by a polarizer. The laser beam was then focused into the fiber core by a $100\times$ oil objective ($\text{NA} = 1.25$). The pitch of the two FBGs was designated to be $2.412 \mu\text{m}$, which corresponds to the 4th Bragg resonant wavelength at $\sim 1550 \text{ nm}$. The length of the two FBGs was 1.071 mm , the length of the laser-inscribed line was set at $15 \mu\text{m}$, and the fiber was translated at a speed of 0.15 mm/s in directions perpendicular to the fiber axis. The wavelength of the phase-shifted peak shown in the figure is located at $\sim 1549.180 \text{ nm}$, the full-width minimum is $\sim 0.642 \text{ nm}$, and the insert loss is $\sim 8 \text{ dB}$. The generation of the phase-shifted peak is considered as the result of F-P interference with a pair of FBG reflectors.

3. Axial Strain Measurement

For comparison purposes, three different PS-FBGs were fabricated using this method. Their respective sizes are clearly shown in Table 1. In order to test the axial-strain response of these PS-FBGs, they were fixed between two translation stages with an initial distance of 20 cm . One of the stages was then moved with a step size of $10 \mu\text{m}$, corresponding to an axial-strain change of $50 \mu\epsilon$ per step [20]. Fig. 2 shows optical microscope images of these three samples and their corresponding transmission spectral evolution with the application of variable axial strain. The phase-shift peak and the FBG resonant dip were each observed to exhibit a significant red shift as the axial strain increased. The red shift of both phase-shift peak and FBG resonant dip is attributed to the elasto-optical effect. Interestingly, in contrast to the PS-FBG without a taper (sample 1), the red-shift amplitude of the phase-shift peak was larger than the FBG resonant dip for a PS-FBG with a taper. As such, significant changes in phase shift can be monitored when a varying amount of axial strain is applied to the PS-FBG with a taper.

Fig. 3 shows experimental data and a linear fit between the wavelength of the phase-shifted peak and the axial strain. The figure also demonstrates that the wavelength of the phase-shifted peak is linearly proportional to changes in the axial strain. The sensitivities of these three samples were measured to be $0.949 \text{ pm}/\mu\epsilon$, $2.37 \text{ pm}/\mu\epsilon$, and $4.59 \text{ pm}/\mu\epsilon$, respectively. The axial strain sensitivity of the phase-shifted peak could be enhanced by decreasing the core diameter.

4. Discussion on the Tunable Phase Shift

When axial strain was applied to this device, an equal load was distributed along each section of the fiber, depending on the local mechanical resistance. The strain loads applied to the tapered and non-tapered areas were equal [20], resulting in the following two equations:

$$\epsilon_s EA_S = \epsilon_T EA_T \quad (1)$$

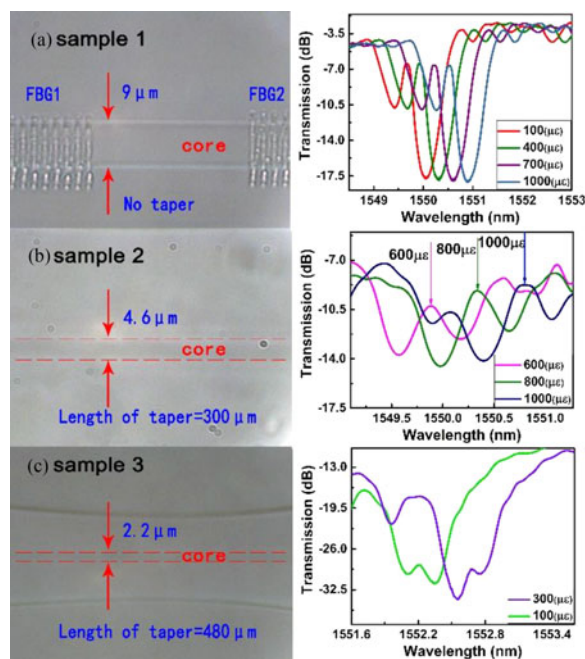


Fig. 2. (a) Optical microscope images and transmission spectral evolution for the first sample, (b) Optical microscope images and transmission spectral evolution for the second sample, (c) Optical microscope images and transmission spectral evolution for the third sample.

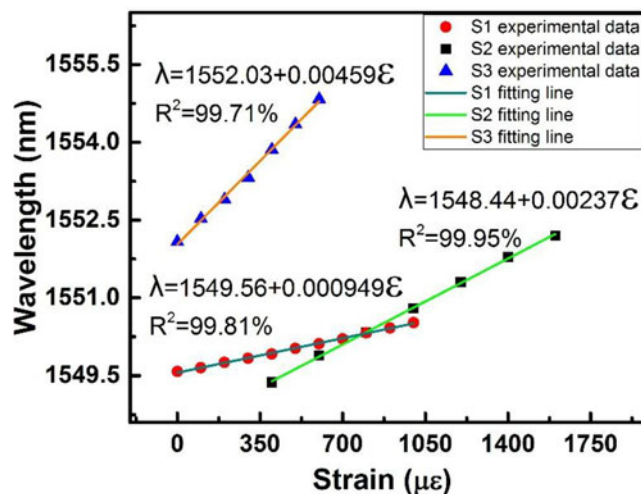


Fig. 3. Experimental data and a fitting relationship between phase-shifted peak wavelength and the axial strain.

Here, ε_S and ε_T represent the axial strain density for the SMF and the taper, A_S and A_T are the cross-sectional area of the SMF and the taper, and E is the elasticity modulus. Obviously, the SMF without a taper has a uniform strain distribution. Fig. 4 demonstrates a simulated distribution of the axial strain density for a tapered fiber using Solidworks. In this simulation, the fiber material is silica, whose elasticity modulus was set to $112,400 \text{ N/mm}^2$, the taper length was $500 \mu\text{m}$, and the radius of the un-tapered and tapered areas were $62.5 \mu\text{m}$ and $15 \mu\text{m}$, respectively. The right end was fixed and an axial strain of 10 N was applied to the structure. It can be seen in Fig. 4 that the axial strain was concentrated at the taper area leading to a larger refractive index change due to elasto-optical effect.

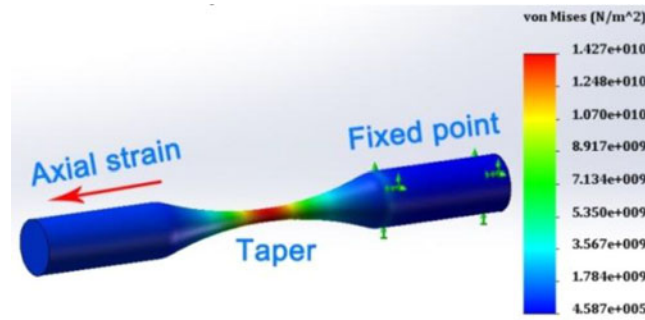


Fig. 4. A simulated distribution of axial strain along the fiber and the axial strain density concentrated in the tapered area.

The presented PS-FBG can be considered as an F-P interferometer (FPI) with a pair of FBG reflectors. The operation wavelength of the FBG and FPI can be expressed as:

$$\lambda_{FBG} = 2n\Lambda \quad (2)$$

$$\lambda_{FPI} = \frac{2nL}{m} \quad (3)$$

where n is the effective refractive index of fiber, Λ is the pitch of FBG, L is the length of F-P cavity (the distance between two FBGs) and m is an integer. Therefore, the axial strain response of λ_{FBG} and λ_{FPI} can be expressed as:

$$\frac{d\lambda_{FBG}}{d\varepsilon} = \frac{\lambda_{FBG}}{n} \frac{dn}{d\varepsilon} \quad (4)$$

$$\frac{d\lambda_{FPI}}{d\varepsilon} = \frac{\lambda_{FPI}}{n} \frac{dn}{d\varepsilon} \quad (5)$$

For the non-tapered configuration, the wavelength change of the phase-shifted peak and the FBG dip are both proportional to $dn/d\varepsilon$ with the same sensitivity of $\lambda dn / n d\varepsilon$, where ε is the axial strain. For the tapered configuration in Fig. 4, the refractive index change of the tapered area was larger than that of the surrounding FBG, due to a concentrated axial strain-induced elasto-optical effect. As such, the degree of phase-shift in the PS-FBG can be adjusted by changing the axial strain.

5. Discussion on the Strain Sensitivity

The phaseshift is mainly caused by the refractive index change of the taper when axial strain was applied to this device. Because the wavelength change of the phase-shift peak induced by the given axial strain $\Delta\lambda \propto \Delta n \propto \varepsilon$, we can obtain the following relation:

$$\frac{d\lambda_T}{d\varepsilon} = \frac{\varepsilon_T}{\varepsilon_S} = \frac{A_S}{A_T} = \frac{r_S^2}{r_T^2} \quad (6)$$

Here, $d\lambda_T/d\varepsilon$ and $d\lambda_S/d\varepsilon$ denote the strain sensitivities of the PS-FBGs with and without a taper, respectively. The relationship between the strain sensitivity and taper radius is demonstrated in Fig. 5.

Because the core diameter of the fiber is gradual along the fiber axis, an equivalent cylinder model was used to replace the taper in the simulation, as shown in Fig. 6.

In this model, circle O_3 is tangent to circle O_1 and the left solid line. Circle O_3 and circle O_4 are asymmetric about the vertical dashed line. From this, we can acquire the profile of the taper, which is marked by the green line. If the radius of the circle O_1 is much larger than that of circle O_3 , we can simplify Fig. 6(a) into Fig. 6(b). In Fig. 6(b), $|A-D|$ is the minimum radius of the fiber core, $|B-C|$ is the maximum radius of the fiber core which is equal to the core radius of SMF, and $|A-B|$ is half

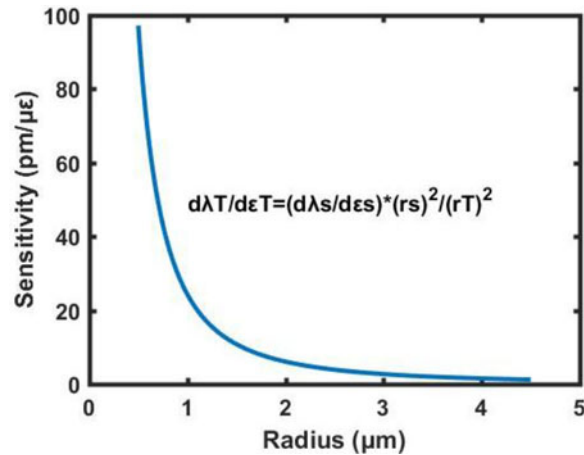


Fig. 5. The relationship between the strain sensitivity and taper radius.

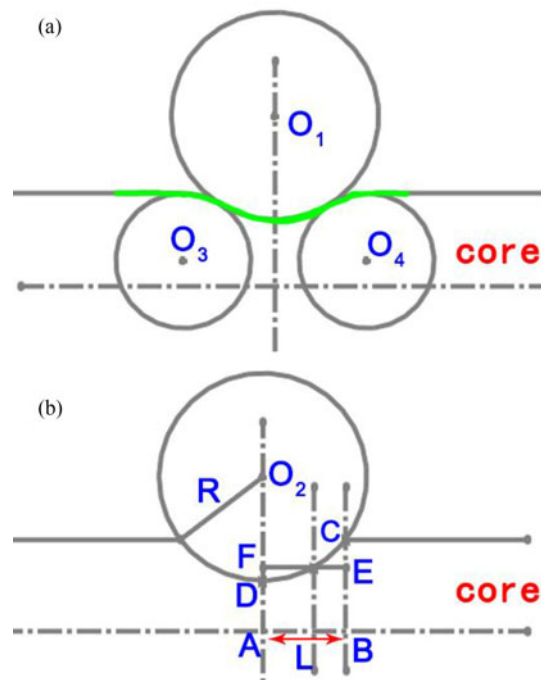


Fig. 6. (a) The equivalent cylinder model of the taper; (b) The simplified model of the taper.

the length of the taper. Theoretically, we can find a rectangle ABEF which has the same area as ABCD. Therefore, the taper could be equivalent to a cylinder with a radius of $|A-F|$ and a length of $2|A-B|$. Point A can be set as the origin of the coordinate system, while the right and upward orientations are set to positive. Analytic formula of circle O_2 and the geometric relation in Fig. 6(b) can be expressed as:

$$R^2 = x^2 + (y - R - R_{\min})^2 \quad (7)$$

$$R'L = \int_0^L \left(-\sqrt{R^2 - x^2} + R + R_{\min} \right) dx \quad (8)$$

$$R^2 = L^2 + (R - R_{\max} + R_{\min})^2 \quad (9)$$

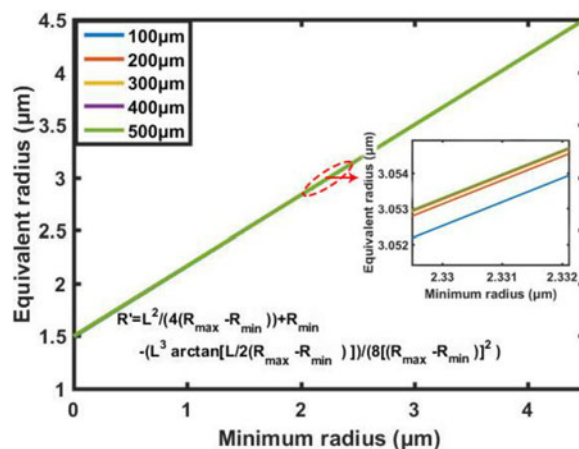


Fig. 7. The relationship between the equivalent radius (R') and the minimum radius (R_{\min}) when the taper length is from $100 \mu\text{m}$ to $500 \mu\text{m}$ and the inset is the local enlarged image that demonstrates R_{\min} plays a leading role to R' .

Combining (7)–(9), we can obtain the following relation

$$R'L = -\frac{L\sqrt{R^2 - L^2}}{2} - \frac{R^2 \arctan \frac{L}{R}}{2} + L(R_{\min} + R) \quad (10)$$

Where R is the radius of circle O_2 , L is the length of $|A - B|$, R' is the equivalent radius of the tapered core, and R_{\max} and R_{\min} are the maximum and minimum radius of the tapered core ($R \gg L \gg R_{\max} > R_{\min}$). After simplification and approximation, the equivalent radius R' can be expressed as:

$$R' = \frac{L^2}{4(R_{\max} - R_{\min})} - \frac{L^3 \arctan \left[\frac{L}{2(R_{\max} - R_{\min})} \right]}{8(R_{\max} - R_{\min})^2} + R_{\min} \quad (11)$$

Fig. 7 shows the relationship between the equivalent radius (R') and the minimum radius (R_{\min}) when the taper length is from $100 \mu\text{m}$ to $500 \mu\text{m}$ and the inset is the local enlarged image that demonstrates R_{\min} plays a leading role to R' . In Fig. 2(b) and (c), taper R' is calculated to be $3.033 \mu\text{m}$ and $2.233 \mu\text{m}$ and the sensitivities are calculated to be $2.64 \text{ pm}/\mu\epsilon$ and $4.87 \text{ pm}/\mu\epsilon$ according to (6). Here, the strain sensitivity of the PS-FBGs without a taper is calculated to be $1.21 \text{ pm}/\mu\epsilon$ by use of the method in [21]. The relative deviation between the calculated and measured sensitivities is less than 10%.

6. Conclusion

We have demonstrated a novel PS-FBG induced by femtosecond laser micromachining. A fiber taper was first fabricated using an arc discharge in a fiber splicer and then two FBG sections were fabricated with femtosecond laser line-by-line inscription on both sides of the taper. It was observed that the amount of phase-shift in the PS-FBG could be adjusted by varying the strain and that strain sensitivity could be enhanced by using a thinner taper. An equivalent model for the taper was developed in order to study the theoretical taper strain response with different radii. These calculated results were in excellent agreement with experiment.

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